

Op-amp based algebra.

Multiplication: non-inverting amp.

Addition: summing amp + inverting amp.

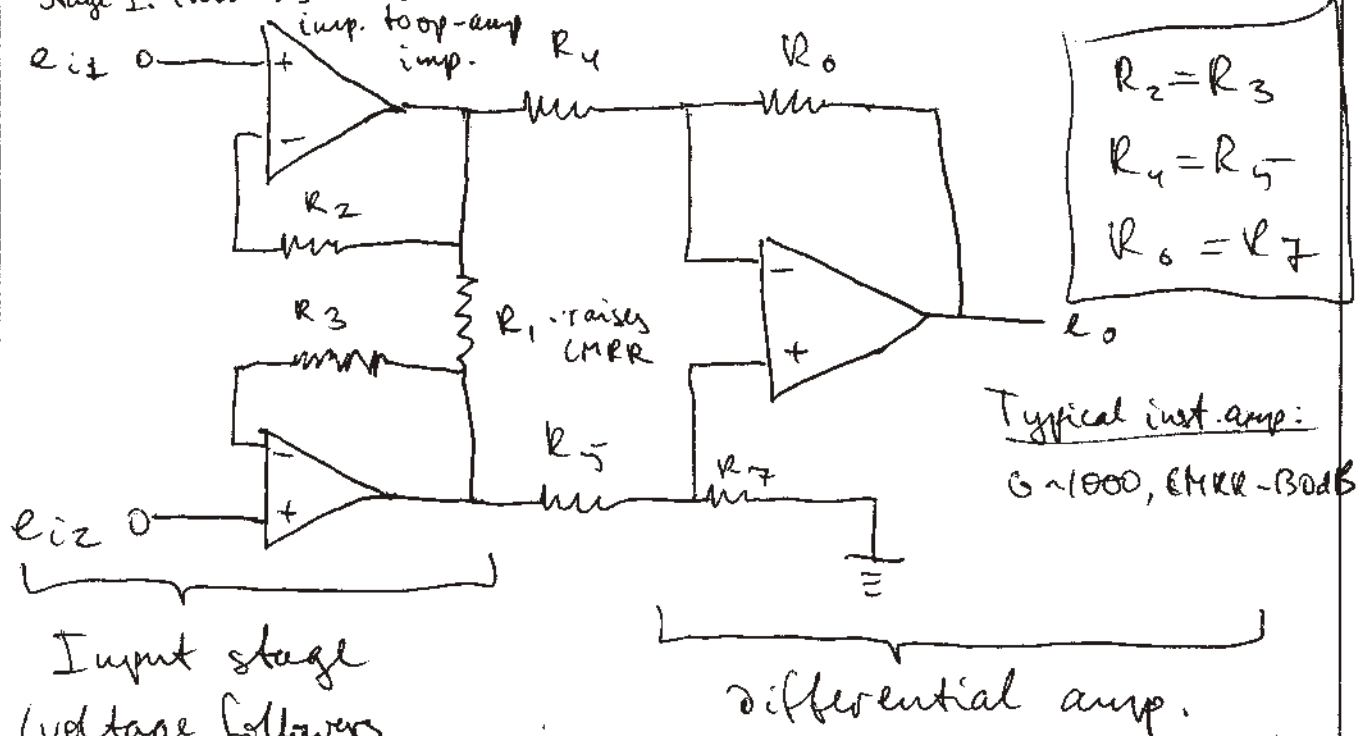
Subtraction: inverting amp (for one input) + summing amp.
Can implement analog computing.

Special amplifier circuits (7.18)

Instrumentation amps. have char. of:

- * accurate amplification of small-voltage diffs. in presence of huge CM signal
- * avoid loading the transducer by keeping current thru it small as possible

Stage 1: increases transducer



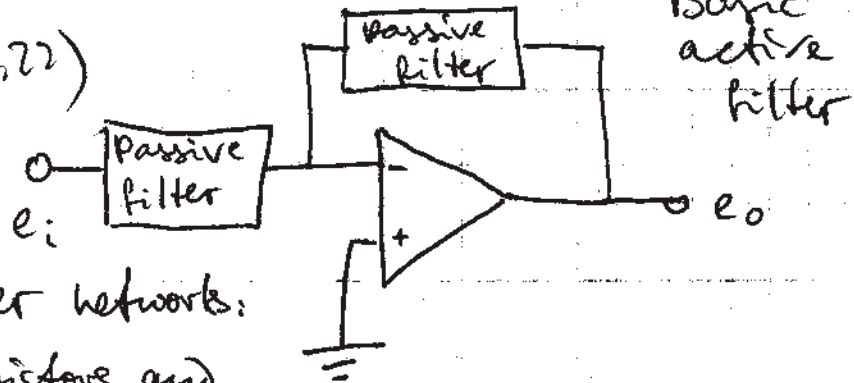
Input stage
(voltage followers
w/ $R_1 \rightarrow \infty$)

differential amp.

$$G = \left(1 + \frac{2R_2}{R_1} \right) \frac{R_6}{R_4}$$
$$e_o = G(e_{i1} - e_{i2})$$

Additional uses of op amps (7.22, 7.23)

Filtering (7.22)

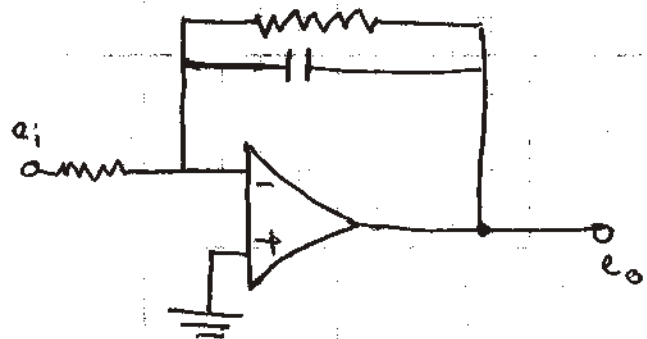
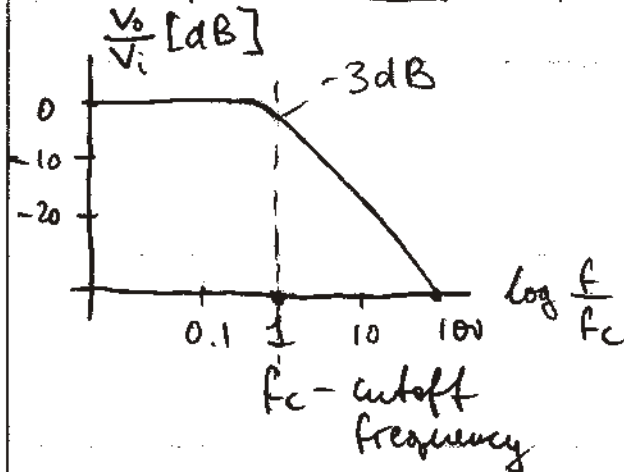


Passive filter networks:

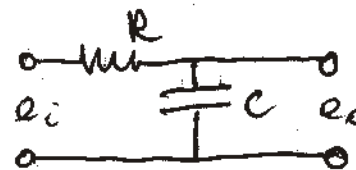
- built from resistors and capacitors
- do not have explicit inductive characteristics (unlike LC filters)

Examples of active filters

Low-pass filter: suppresses high-frequency components



(compare with unpowered RC low-pass filter:



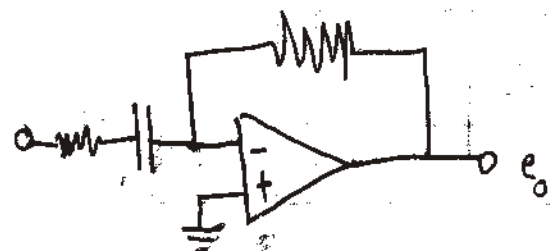
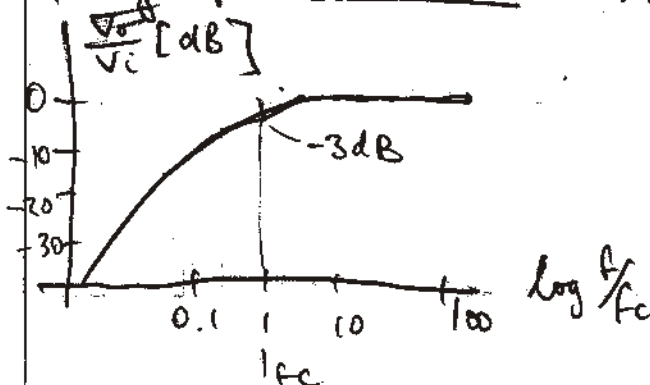
$$f_c = \frac{1}{2\pi RC}$$

frequency response

High-pass filter:

suppresses low frequency.

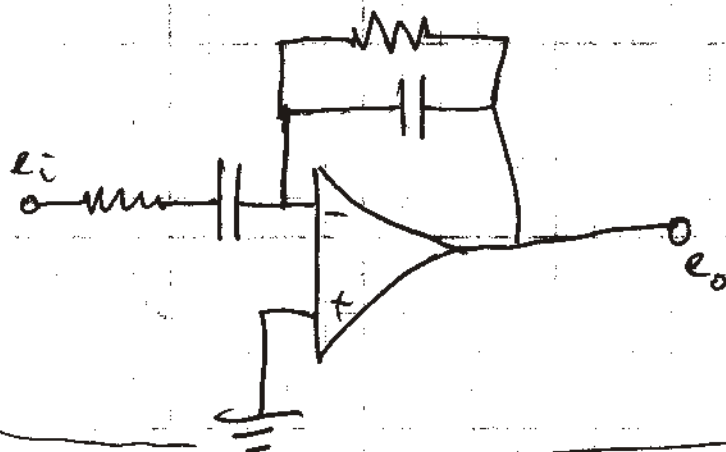
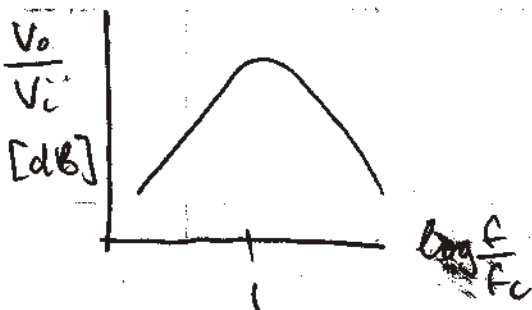
$$\frac{V_o}{V_i} = \frac{1}{\sqrt{1 + \left(\frac{f}{f_c}\right)^2}}$$



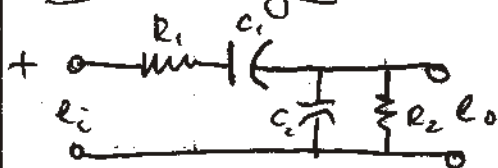
Corresponding RC filter would be...



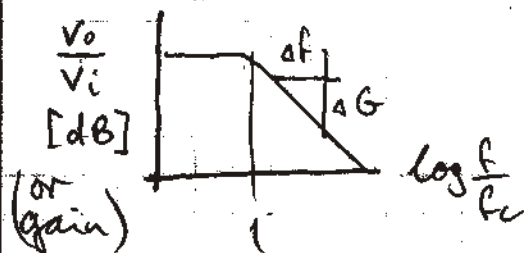
Band-pass filter (chops out low and high freq.)



RC analog



What's good about active filters compared w/ RC or LC?



Roll-off: $\frac{\Delta G}{\Delta f}$ in terms of $\frac{dB}{octave}$ or $\frac{dB}{decade}$

Decade = frequency change by a factor of 10

Octave = 1 ————— 2

Roll-off for RC filters: $\sim 6 \frac{dB}{octave}$.

active filters: $\sim 80 \frac{dB}{octave}$.

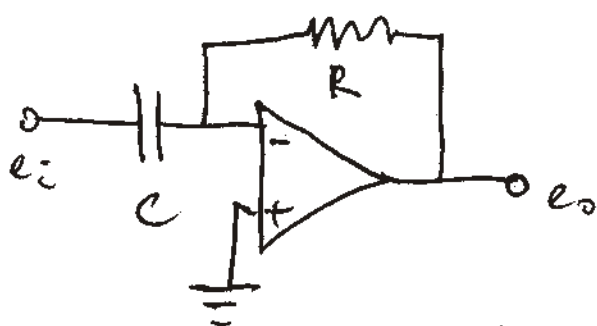
Differentiators & Integrators (7.23)

Addition to "op amp algebra".

Respond to:

- rate of change of input
- or
- time history of input

Op. amp. Differentiator



Currents through R and C are equal (impedance of op amp is HUGE).

$$e_- = e_+ = 0.$$

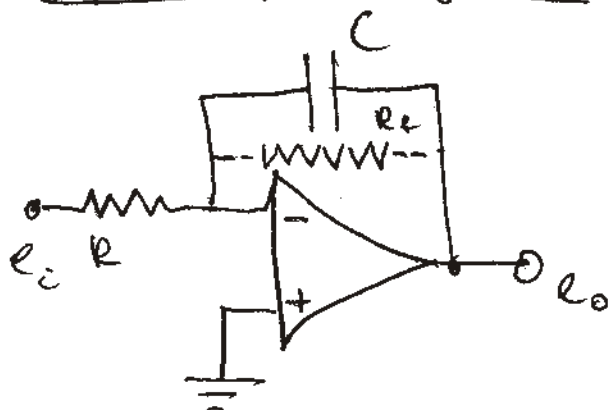
$$C \frac{d}{dt} (e_i - 0) = \frac{0 - e_o}{R}.$$

$\Downarrow$

$$e_o = -RC \frac{d}{dt} e_i$$

Output = time derivative of input $\times$ const

Op. amp. Integrator



From resistor and capacitor current equality (again),

$$\frac{e_i}{R} = -C \frac{d}{dt} e_o.$$

Integrate:

$$e_o = -\frac{1}{RC} \int e_i dt + \text{const.}$$

R_f - may be placed in parallel w/ C.
large resistor.

* Prevents drift in capacitor charge over long-time intervals

* Restricts signal frequencies to $f \gg \frac{1}{2\pi R_f C}$.